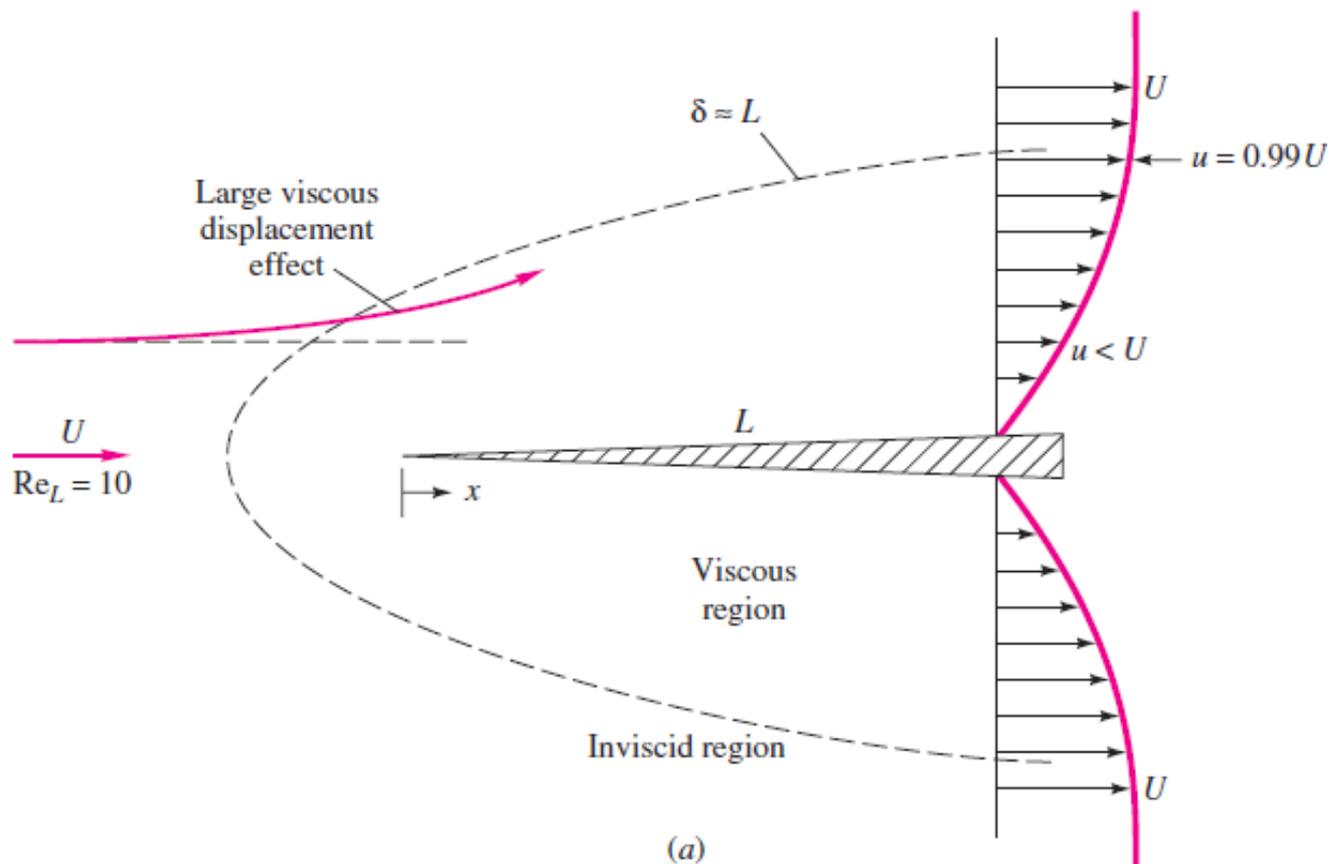


# Noções de Escoamentos Externos

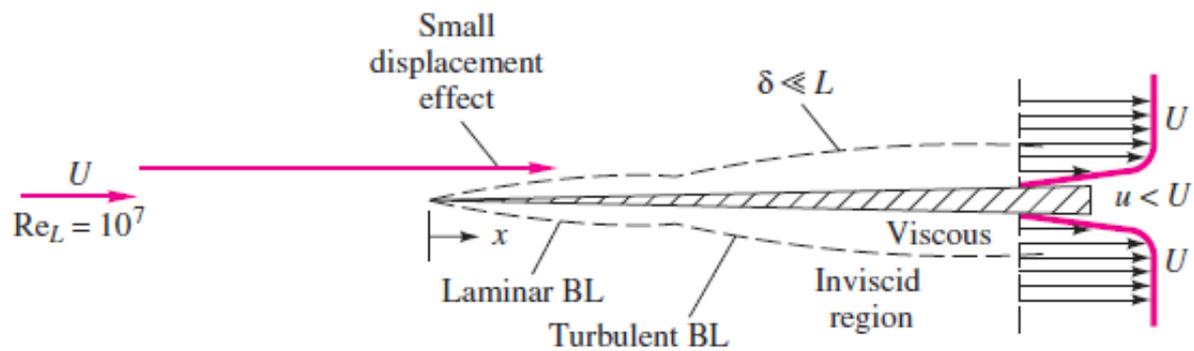
Ref: White F.M., Mecânica dos  
Fluidos

# Introdução

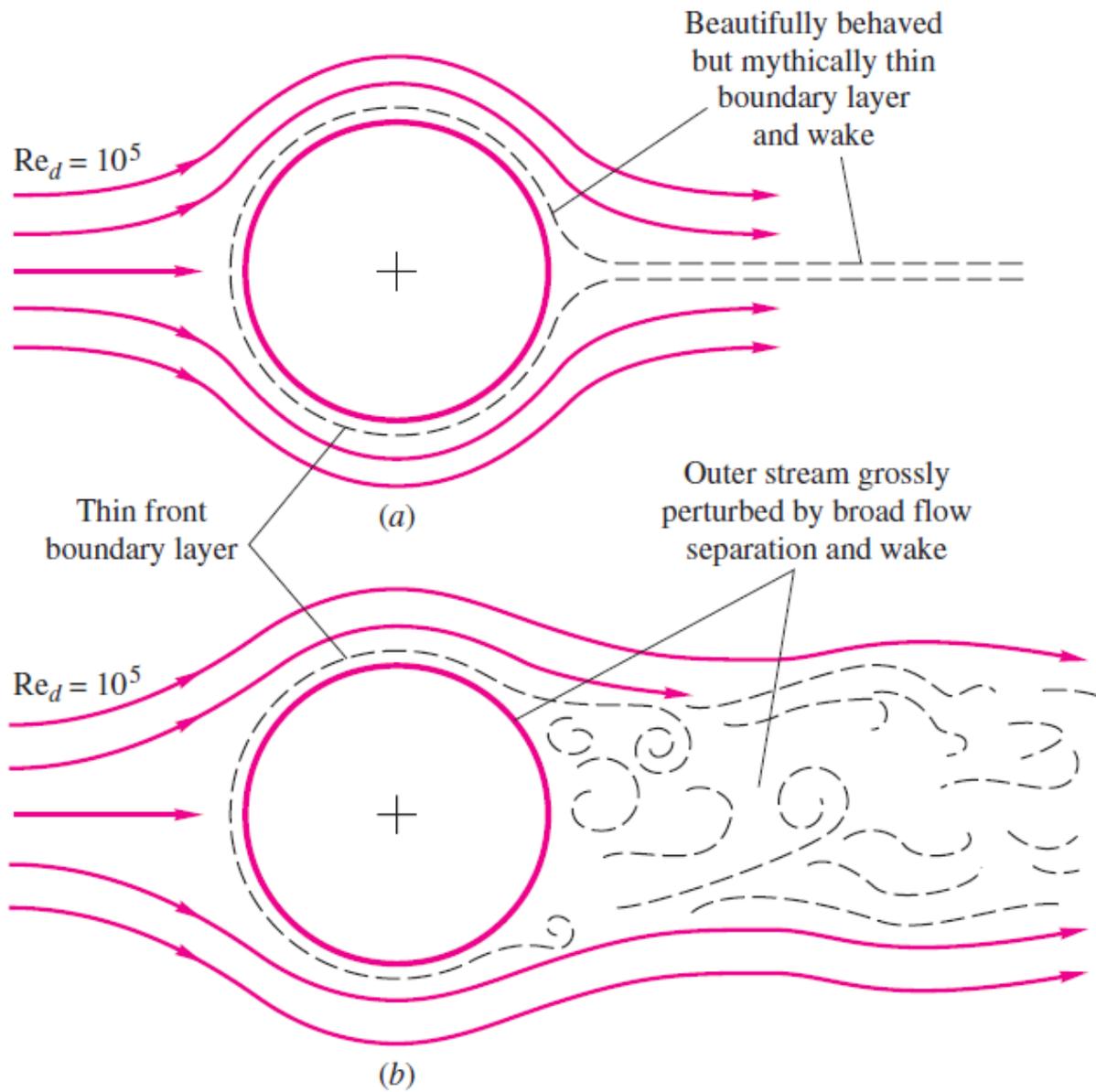
- Veremos aqui apenas algumas noções
  - Como de costume, maior ver notas de aula (lousa)
- Veremos escoamentos externos mais a fundo em Mecânica dos Fluidos II (EM561)



(a)



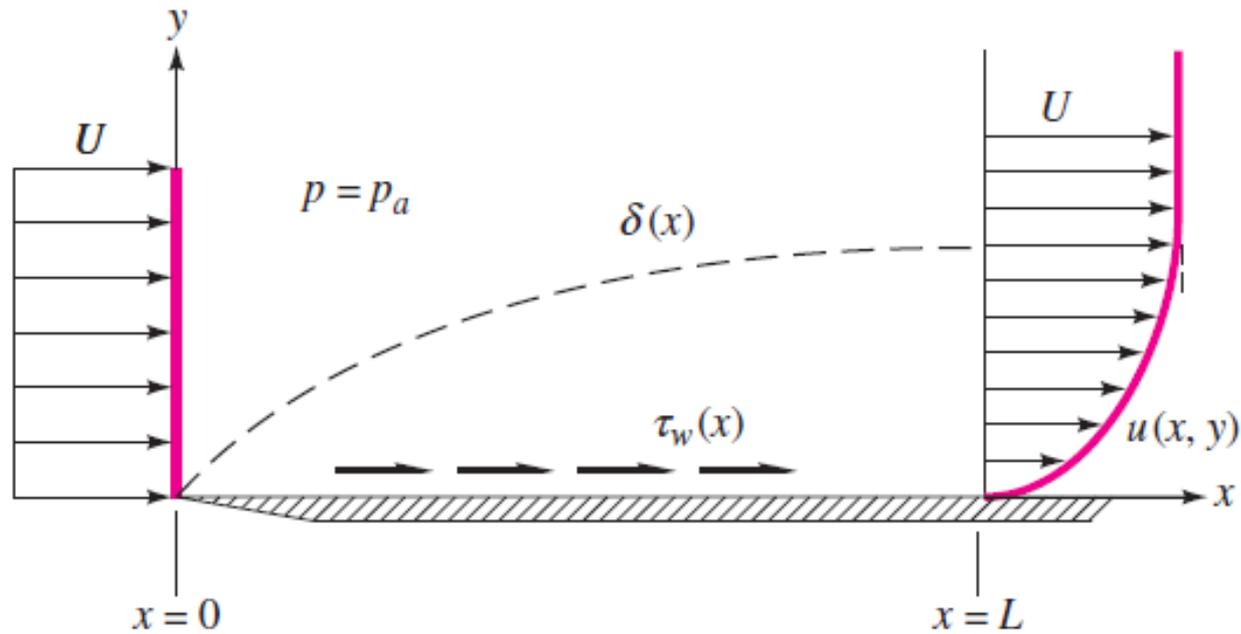
(b)



Exemplo: <https://youtu.be/SiOiVHUEYao?si=6p0tPmCcYb4cGPFC>

# Placa plana

- Obtemos a seguir as seguintes expressões para placa plana, utilizando o V.C. mostrado em aula:
  - Força de arrasto
  - Tensão na parede
  - Coeficiente de fricção
  - Coeficiente de arrasto



$$D(x) = \rho b \int_0^{\delta(x)} u(U - u) dy$$

$$D(x) = \rho b U^2 \theta \quad \theta = \int_0^{\delta} \frac{u}{U} \left( 1 - \frac{u}{U} \right) dy$$

$$\tau_w = \rho U^2 \frac{d\theta}{dx}$$

$$c_f = \frac{2\tau_w}{\rho U^2} = 2 \frac{d\theta}{dx}$$

$$C_D = \frac{2D(L)}{\rho U^2 b L} = 2 \frac{\theta}{L}$$

$$D = \frac{1}{2} C_D \rho U^2 b L$$



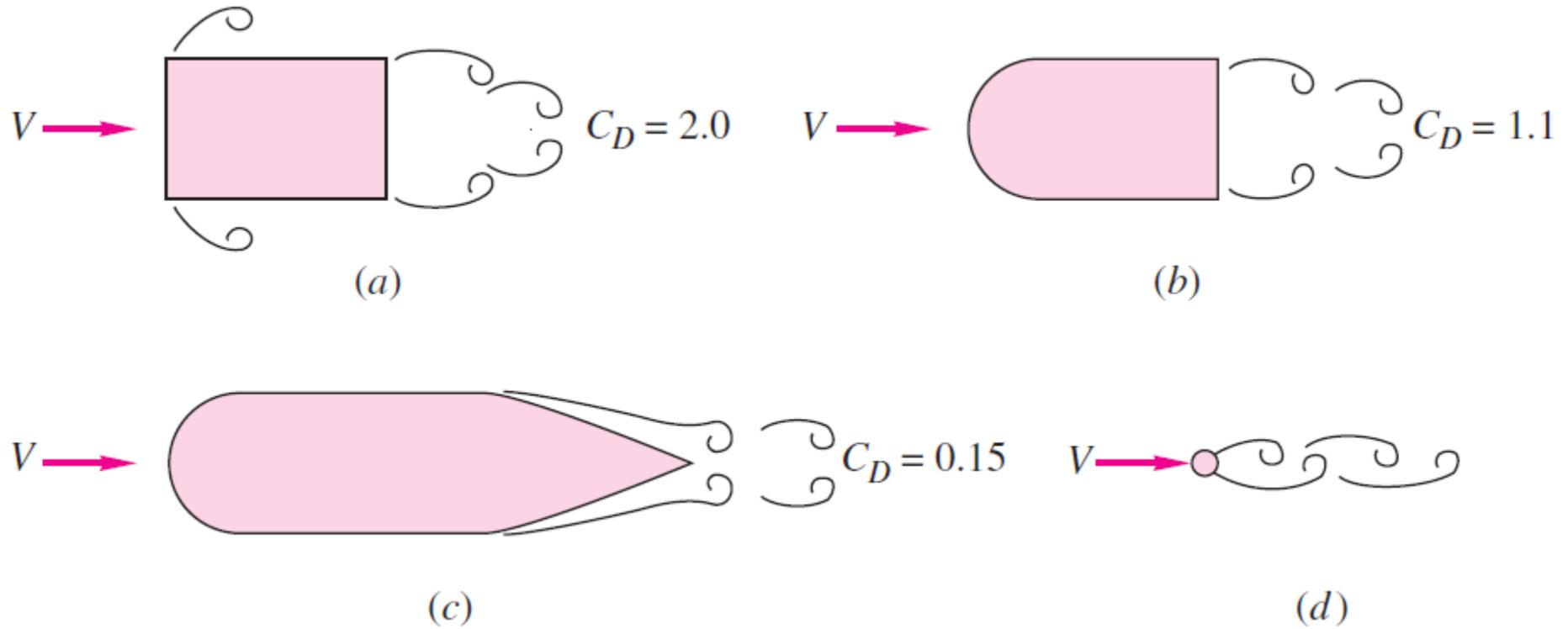
ARRASTO

# Corpo rombudo

- Há arrasto viscoso e arrasto de pressão

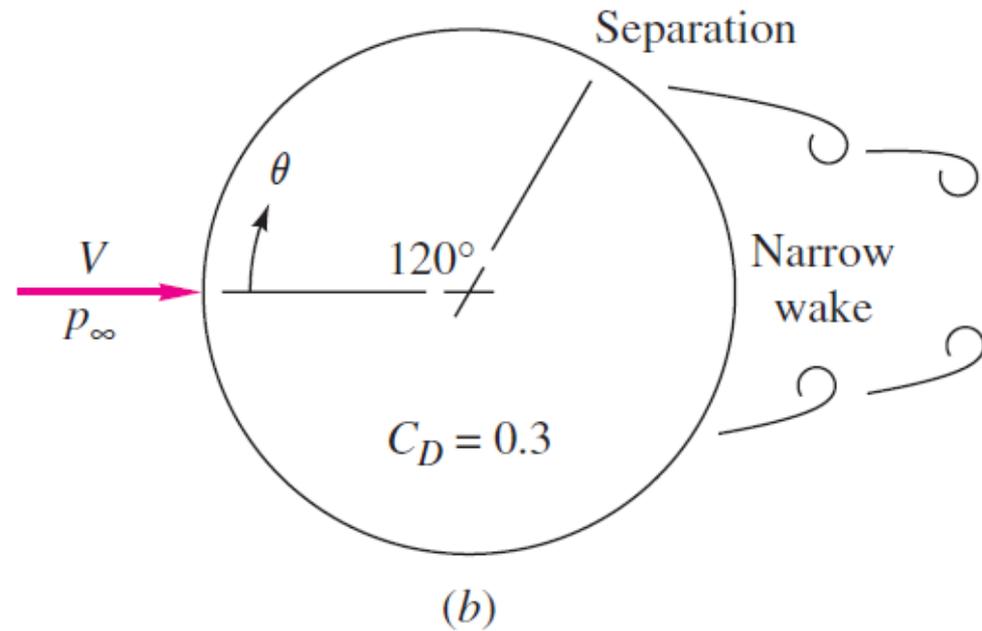
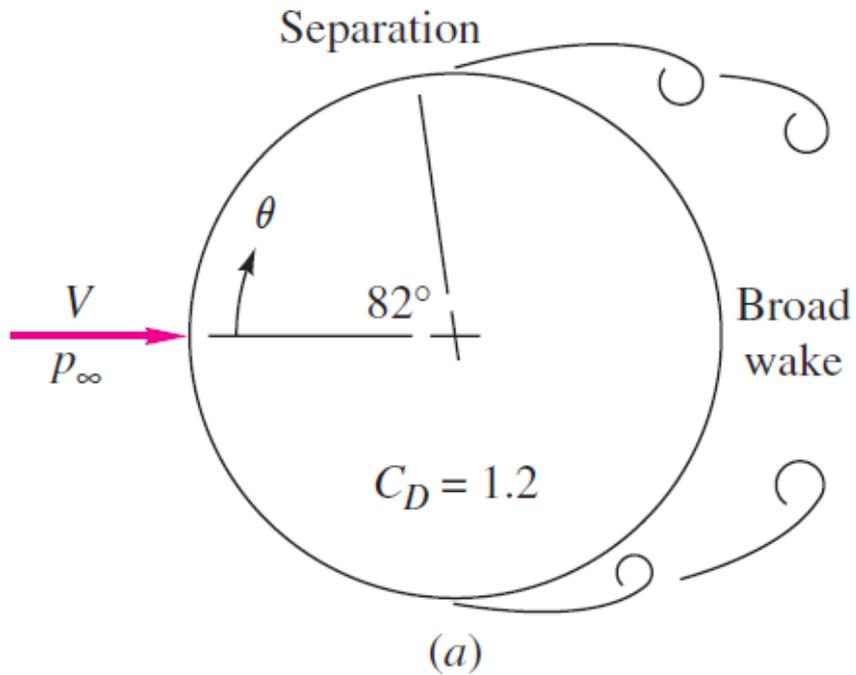
$$C_D = C_{D,\text{press}} + C_{D,\text{fric}}$$

- Em geral o arrasto de pressão é muito maior
  - Nestes casos, nos preocupamos apenas com o arrasto de pressão.

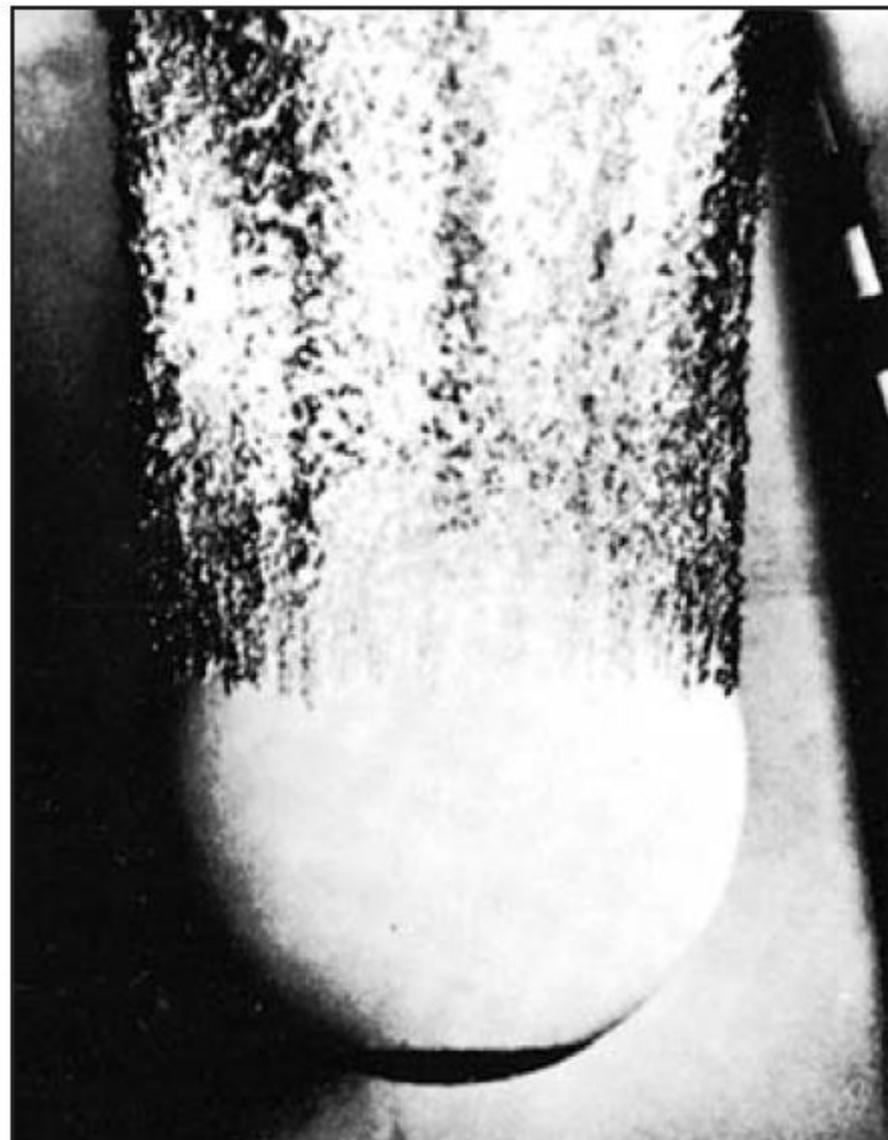
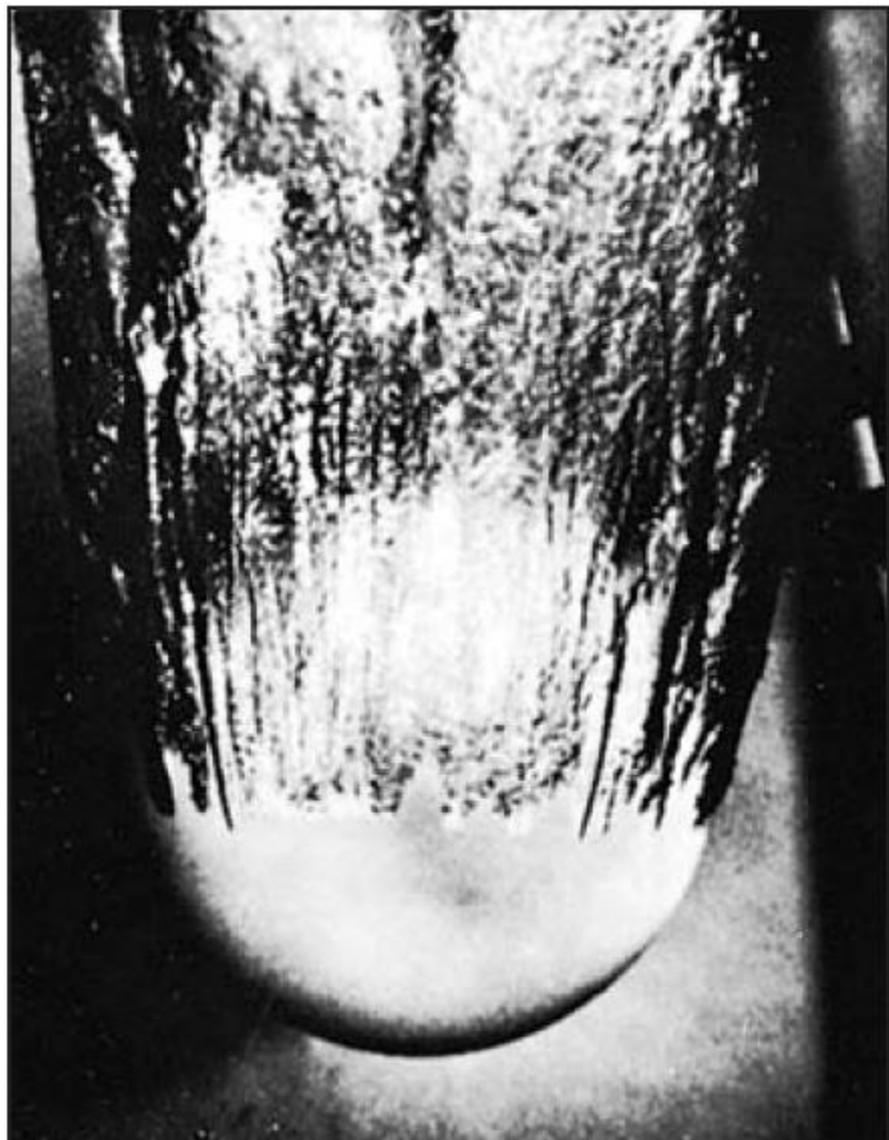


Exemplo (escoamentos externos em corpos rombudos)

<https://youtu.be/bJX8fVsQ5oQ?si=-C7cKez1mU8PBQug>



Exemplo: <https://youtu.be/B2jz4MJAtSw?si=ZGu-YVcGKoIb0F2K>



## $C_D$ Placa Plana

Laminar

$$C_D = \frac{1.328}{\text{Re}_L^{1/2}}$$

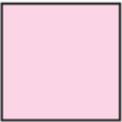
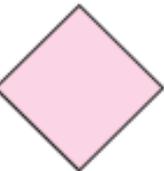
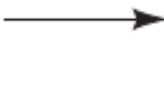
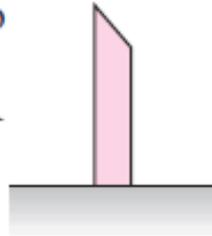
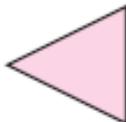
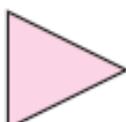
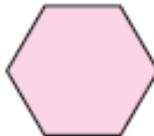
Turbulento

$$C_D \approx \begin{cases} \frac{0.031}{\text{Re}_L^{1/7}} - \frac{1440}{\text{Re}_L} \\ \frac{0.031}{\text{Re}_L^{1/7}} - \frac{8700}{\text{Re}_L} \end{cases}$$

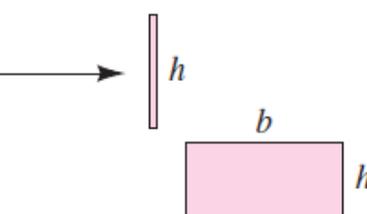
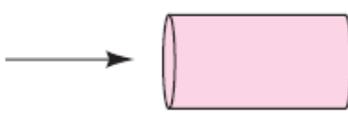
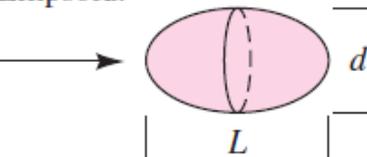
$$\text{Re}_{\text{trans}} = 5 \times 10^5$$

$$\text{Re}_{\text{trans}} = 3 \times 10^6$$

# $C_D$ Corpo Rombudo

Shape	$C_D$ based on frontal area	Shape	$C_D$ based on frontal area	Shape	$C_D$ based on frontal area
Square cylinder:		Half cylinder:		Plate:	
 	2.1	 	1.2	 	2.0
 	1.6	 	1.7	Thin plate normal to a wall:	
Half tube:		Equilateral triangle:		 	1.4
 	1.2	 	1.6	Hexagon:	
 	2.3	 	2.0	 	1.0  0.7

# $C_D$ Corpo Rombudo

Body	Ratio	$C_D$ based on frontal area		Body	Ratio	$C_D$ based on frontal area																	
Rectangular plate: 	$b/h$ 1 5 10 20 $\infty$	1.18 1.2 1.3 1.5 2.0		Flat-faced cylinder: 	$L/d$ 0.5 1 2 4 8	1.15 0.90 0.85 0.87 0.99																	
Ellipsoid: 	$L/d$ 0.75 1 2 4 8	<table border="1"> <thead> <tr> <th></th> <th>Laminar</th> <th>Turbulent</th> </tr> </thead> <tbody> <tr> <td>0.75</td> <td>0.5</td> <td>0.2</td> </tr> <tr> <td>1</td> <td>0.47</td> <td>0.2</td> </tr> <tr> <td>2</td> <td>0.27</td> <td>0.13</td> </tr> <tr> <td>4</td> <td>0.25</td> <td>0.1</td> </tr> <tr> <td>8</td> <td>0.2</td> <td>0.08</td> </tr> </tbody> </table>		Laminar	Turbulent	0.75	0.5	0.2	1	0.47	0.2	2	0.27	0.13	4	0.25	0.1	8	0.2	0.08		Buoyant rising sphere [50], $135 < Re_d < 1E5$	$C_D \approx 0.95$
	Laminar	Turbulent																					
0.75	0.5	0.2																					
1	0.47	0.2																					
2	0.27	0.13																					
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